

13+ Entrance Scholarships

MATHEMATICS 1

30 January 2018
Time allowed – 1 hour

You may try the questions in any order

No calculating aids may be used

Show all working

Total 100 marks

1 a. Work out exactly

i.
$$3.87 \times 50.7$$
 (3 marks)

ii.
$$234.65 \div 9.5$$
 (4 marks)

b. Give the answers to the following as fractions in their simplest form

i.
$$\frac{17}{36} - \frac{1}{4}$$
 (3 marks)

ii.
$$4\frac{2}{3} \div \frac{7}{12}$$
 (3 marks)

2 Work out as simply as possible

a.
$$82^2 - (37 \times 82) + (82 \times 5)$$
 (4 marks)

b.
$$513^2 - 487^2$$
 (4 marks)

c.
$$\frac{320^2 - (640 \times 150)}{16^2 \times 5^2}$$
 (5 marks)

3 a. Multiply out and simplify

i.
$$(3a + 2b)^2$$
 (4 marks)

ii.
$$(12x^2 + 3xy - 2y^2)(y - x)$$
 (4 marks)

b. Factorise fully

i.
$$48a^3b^2 - 27a^2b^4$$
 (3 marks)

ii.
$$48z^4 - 3y^2$$
 (3 marks)

iii.
$$x^2 + 15x + 54$$
 (2 marks)

c. Simplify

i.
$$\frac{4y^2 - 4x^2}{2yz - 2xz}$$
 (4 marks)

ii.
$$(3xy^2)^2 \div \frac{y^3}{x}$$
 (3 marks)

4 Solve each of these equations for x

a.
$$8(x-3)-2(x+3)=12$$
 (3 marks)

b.
$$\frac{3x-3}{2} + \frac{3x+2}{5} = 22$$
 (4 marks)

c.
$$(2x+6)(x+3) - (x+2)^2 = 7$$
 (5 marks)

Rearrange the following formula to make x the subject

$$d. \quad \frac{4d}{x-b} = \frac{3b}{x-a} \tag{5 marks}$$

5 Solve each of these pairs of equations for x and y

a.
$$4x - 3y = 13$$

 $5x - 2y = 25$ (5 marks)

b.
$$\frac{1}{3}x + \frac{1}{2}y = 4$$

$$\frac{2}{5}x - \frac{1}{4}y = -\frac{3}{10}$$
(6 marks)

6. Solve each of these equations for *x* using algebraic methods.

a.
$$x^2 - 9x - 22 = 0$$
 (4 marks)

b.
$$4x^2 - 4x - 3 = 0$$
 (5 marks)

c.
$$\frac{x}{2} + \frac{3}{x-1} = 3$$
 (6 marks)

d.
$$\frac{42}{x+1} - \frac{20}{x-3} = 1$$
 (8 marks)

Total 100 marks