RADLEY COLLEGE Entrance Scholarships



MATHEMATICS I

March 2006

Time allowed 1 hour

You may try the questions in any order.

No calculating aids may be used.

Show all working.

1. a) Work out exactly

i)
$$7.05 \times 96.2$$
 (3 marks)

ii)
$$3.6288 \div 0.28$$
 (3 marks)

b) Give the answers to the following as fractions in their simplest form

i)
$$\frac{5}{8} + \frac{1}{24}$$
 (3 marks)

ii)
$$3\frac{3}{5} \times 2\frac{4}{9}$$
 (3 marks)

iii)
$$\left(4\frac{1}{3} - 2\frac{3}{4}\right) \div 1\frac{3}{16}$$
 (4 marks)

2. Work out as simply as possible

a)
$$562^2 - 438^2$$
 (4 marks)

b)
$$(34 \times 89) + 34^2 - (23 \times 34)$$
 (4 marks)

c)
$$(89 \times 35) + (65 \times 11) - (11 \times 76) + (54 \times 89)$$
 (4 marks)

d)
$$\frac{(400 \times 306) - 306^2}{3.06 \times 47}$$
 (4 marks)

3. a) Multiply out and simplify

i)
$$(3a+4b)^2$$
 (3 marks)

ii)
$$(3x^2 + 6xy + 12y^2)(x - 2y)$$
 (3 marks)

b) Factorise fully

i)
$$18ab-12a^2b$$
 (3 marks)

ii)
$$18a^2 - 50b^2$$
 (3 marks)

iii)
$$x^2 + 17x + 60$$
 (3 marks)

c) Simplify

i)
$$\frac{x^2 - y^2}{xz + yz}$$
 (3 marks)

ii)
$$\frac{x^2}{y^3} \div \frac{x^3}{y^5}$$
 (3 marks)

4. Solve each of these equations for x

a)
$$8(x+3)-3(x-1)=57$$
 (3 marks)

b)
$$\frac{x+8}{7} + \frac{2x+3}{5} = 5$$
 (4 marks)

c)
$$(3x+1)(x+5)-3x^2=117$$
 (4 marks)

Rearrange the following formula to make *x* the subject

d)
$$\frac{a}{x+b} = \frac{c}{x-d}$$
 (6 marks)

5. Solve each of these pairs of equations for x and y

a)
$$3x + 5y = 19$$
$$4x - 3y = 6$$
 (6 marks)

b)
$$\frac{\frac{1}{8}x + \frac{1}{7}y = 8}{\frac{3}{4}x + \frac{2}{5}y = 32}$$
 (6 marks)

6. Solve each of these equations for x

a)
$$x^2 - 7x - 18 = 0$$
 (4 marks)

b)
$$4x^2 - 8x + 3 = 0$$
 (6 marks)

c)
$$\frac{28}{x-3} - \frac{27}{x+2} = 4$$
 (8 marks)