

13+ Entrance Scholarships

MATHEMATICS I

January 2019
Time allowed – 1 hour

You may try the questions in any order

No calculating aids may be used

Show all your working

Total 100 marks

1 a. Work out exactly

i.
$$2.89 \times 60.7$$
 (3 marks)

ii.
$$274.55 \div 8.5$$
 (5 marks)

b. Give the answers to the following as fractions in their simplest form

i.
$$\frac{19}{21} - \frac{3}{7}$$
 (2 marks)

ii.
$$2\frac{2}{7} \div \frac{3}{14}$$
 (3 marks)

2 Work out as simply as possible

a.
$$73^2 - (49 \times 73) + (73 \times 26)$$
 (4 marks)

b.
$$\frac{489^2 - 479^2}{489 + 479}$$
 (4 marks)

c.
$$(69 \times 13) - (31 \times 18) + (69 \times 56) - (31 \times 13)$$
 (5 marks)

3 a. Multiply out and simplify

i.
$$(4a - 3b)^2$$
 (3 marks)

ii.
$$(x-2y)(4x^2-3xy+2y)$$
 (4 marks)

b. Factorise fully

i.
$$32a^3b^2 - 48a^2b^4$$
 (3 marks)

ii.
$$5y^2 - 80x^4$$
 (4 marks)

iii.
$$x^2 + 14x + 48$$
 (2 marks)

c. Simplify

i.
$$\frac{4x^2-4y^2}{6xz-6yz}$$
 (4 marks)

ii.
$$(4xy^2)^2 \div \frac{2y^3}{x^2}$$
 (3 marks)

4 Solve each of these equations for x

a.
$$4(3-x)-3(2x-2)=8$$
 (3 marks)

b.
$$\frac{3x+4}{2} + \frac{2x+1}{3} = 11$$
 (4 marks)

c.
$$(x^2 + 2)(x + 2) + (3 - 5x) = 7$$
 (6 marks)

Rearrange the following formula to make x the subject

d.
$$\frac{3a-x}{b-x} = \frac{x}{x-a}$$
 (5 marks)

5 Solve each of these pairs of equations for x and y

a.
$$6x - 5y = 38$$

 $4x = 20 + 2y$ (5 marks)

b.
$$\frac{3}{4}x - \frac{1}{2}y = \frac{5}{4}$$

$$\frac{1}{3}x - \frac{1}{4}y = \frac{1}{2}$$
(6 marks)

6. Solve each of these equations for *x* using algebraic methods.

a.
$$x^2 - 11x - 42 = 0$$
 (4 marks)

b.
$$6x^2 - 5x - 6 = 0$$
 (5 marks)

c.
$$\frac{x-3}{4} - \frac{3}{x-7} = 2$$
 (6 marks)

d.
$$\frac{20}{x-3} - \frac{42}{x+7} = 2$$
 (7 marks)

Total 100 marks